

## Motion Graphs

To be able to interpret displacement-time and velocity-time graphs  
 To be able to represent motion with displacement-time and velocity-time graphs  
 To know the significance of the gradient of a line and the area under it.

### Gradient

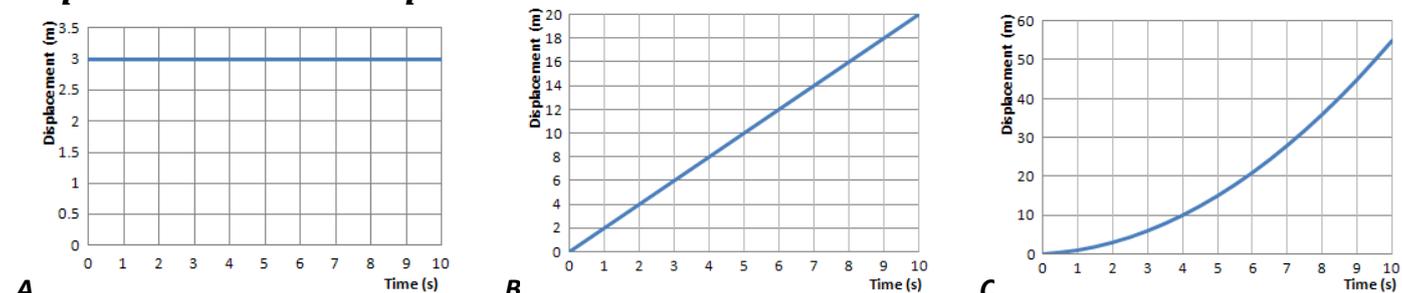
We calculate the gradient by choosing two points on the line and calculating the change in the y axis (up/down) and the change in the x axis (across).

$$\text{gradient} = \frac{\Delta y}{\Delta x}$$

### Area Under Graph

At this level we will not be asked to calculate the area under curves, only straight lines.  
 We do this by breaking the area into rectangles (base x height) and triangles ( $\frac{1}{2}$  base x height).

### Displacement-Time Graphs



Graph A shows that the displacement stays at 3m, it is stationary.  
 Graph B shows that the displacement increases by the same amount each second, it is travelling with constant velocity.  
 Graph C shows that the displacement covered each second increases each second, it is accelerating.

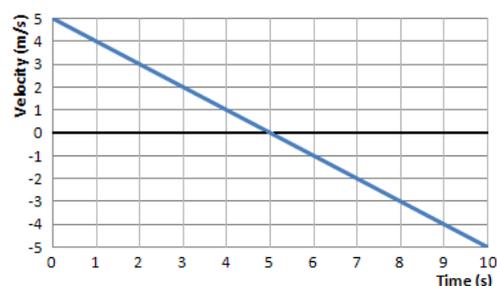
Since  $\text{gradient} = \frac{\Delta y}{\Delta x}$  and  $y = \text{displacement}$  and  $x = \text{time} \rightarrow \text{gradient} = \frac{\Delta s}{\Delta t} \rightarrow \boxed{\text{gradient} = \text{velocity}}$

### Velocity- Time Graphs



Graph A shows that the velocity stays at 4m/s, it is moving with constant velocity.  
 Graph B shows that the velocity increases by the same amount each second, it is accelerating by the same amount each second (uniform acceleration).  
 Graph C shows that the velocity increases by a larger amount each second, the acceleration is increasing (non-uniform acceleration).

Since  $\text{gradient} = \frac{\Delta y}{\Delta x}$  and  $y = \text{velocity}$  and  $x = \text{time} \rightarrow \text{gradient} = \frac{\Delta v}{\Delta t} \rightarrow \boxed{\text{gradient} = \text{acceleration}}$



area = base x height  $\rightarrow$  area = time x velocity  $\rightarrow$

This graph shows the velocity decreasing in one direction and increasing in the opposite direction.

If we decide that  $\leftarrow$  is negative and  $\rightarrow$  is positive then the graph tells us:  
The object is initially travels at 5 m/s  $\rightarrow$   
It slows down by 1m/s every second  
After 5 seconds the object has stopped  
It then begins to move  $\leftarrow$   
It gains 1m/s every second until it is travelling at 5m/s  $\leftarrow$