

## Kirchhoff's Laws and Potential Dividers

To know Kirchhoff's Laws and be able to apply them to questions  
 To know what a potential divider is and be able to calculate the output voltage  
 To be able to explain an application of a potential divider

### Kirchhoff's Laws

Kirchhoff came up with two laws concerning conservation in electrical circuits.

#### First Law

Electric charge is conserved in all circuits, all the charge that arrives at a point must leave it.

In the diagram we can say that:

$$\text{Current going in} = \text{current going out.}$$

$$I_1 = I_2 + I_3 + I_4$$

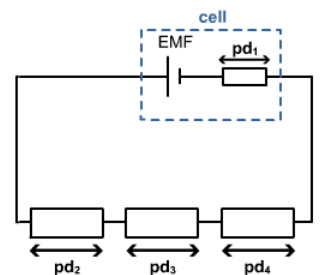
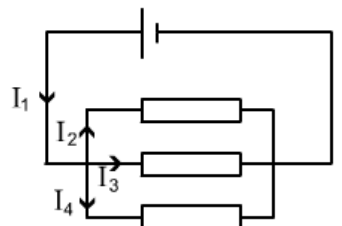
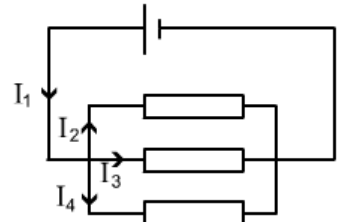
#### Second Law

Energy is conserved in all circuits, for any complete circuit the sum of the emfs is equal to the sum of the potential differences.

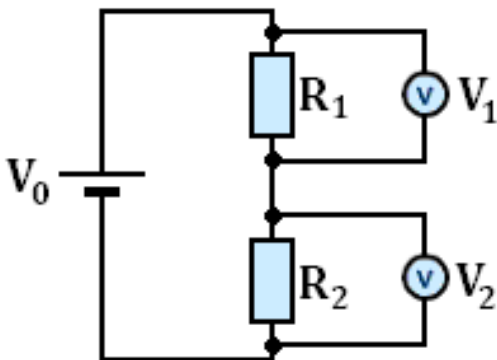
In the diagram we can say that:

$$\text{Energy givers} = \text{energy takers.}$$

$$\varepsilon = \text{pd}_1 + \text{pd}_2 + \text{pd}_3 + \text{pd}_4.$$



### Potential Dividers



A potential divider is used to produce a desired potential difference, it can be thought of as a potential selector.

A typical potential divider consists of two or more resistors that share the emf from the battery/cell.

The p.d.s across  $R_1$  and  $R_2$  can be calculated using the following equations:

$$V_1 = V_0 \frac{R_1}{R_1 + R_2}$$

$$V_2 = V_0 \frac{R_2}{R_1 + R_2}$$

This actually shows us that the size of the potential difference is equal to the input potential multiplied by what proportion of  $R_1$  is of the total resistance.

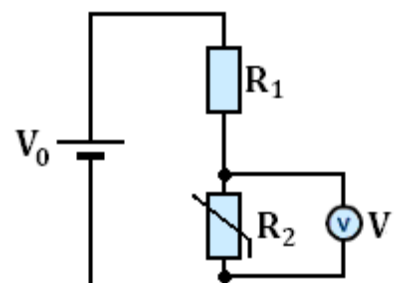
If  $R_1$  is  $10 \Omega$  and  $R_2$  is  $90 \Omega$ ,  $R_1$  contributes a tenth of the total resistance so  $R_1$  has a tenth of the available potential. This can be represented using:

$$\frac{R_1}{R_2} = \frac{V_1}{V_2}$$

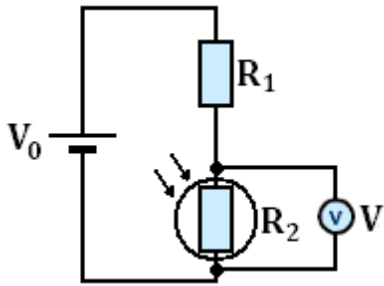
The ratio of the resistances is equal to the ratio of the output voltages.

### Uses

In this potential divider the second resistor is a thermistor. When the temperature is low the resistance ( $R_2$ ) is high, this makes the output voltage high. When the temperature is high the resistance ( $R_2$ ) is low, this makes the



output voltage low. A use of this would be a cooling fan that works harder when it is warm.



In the second potential divider the second resistor is a Light Dependant Resistor. When the light levels are low the resistance ( $R_2$ ) is high, making the output voltage high. When the light levels increase the resistance ( $R_2$ ) decreases, this makes the output voltage decrease. A use of this could be a street light sensor that lights up when the surrounding are dark.