Equations of Motion

To be able to use the four equations of motion
To know the correct units to be used
To be able to find the missing variable: s u v a or t

Defining Symbols

Before we look at the equations we need to assign letters to represent each variable

Displacement	= ***s***	m	metres
Initial Velocity	= ***u***	m/s	metres per second
Final Velocity	= ***v***	m/s	metres per second
Acceleration	= ***a***	m/s^2	metres per second per second
Time	= ***t***	s	seconds

Equations of Motion

Equation 1

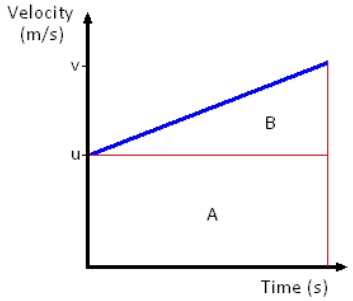
If we start with the equation for acceleration $a = \frac{(v-u)}{t}$ we can rearrange this to give us an equation 1

$at = (v-u)$ → $at + u = v$ $\qquad$ $\boxed{v = u + at}$

Equation 2

We start with the definition of velocity and rearrange for displacement

velocity = displacement / time → displacement = velocity x time



In situations like the graph to the right the velocity is constantly changing, we need to use the average velocity.

displacement = average velocity x time

The average velocity is give by: average velocity = $\frac{(u+v)}{2}$

We now substitute this into the equation above for displacement

displacement = $\frac{(u+v)}{2}$ x time → $s = \frac{(u+v)}{2}t$ $\qquad$ $\boxed{s = \frac{1}{2}(u+v)t}$

Equation 3

With Equations 1 and 2 we can derive an equation which eliminated *v*. To do this we simply substitute $v = u + at$ into $s = \frac{1}{2}(u+v)t$

$s = \frac{1}{2}(u + (u+at))t$ → $s = \frac{1}{2}(2u+at)t$ → $s = \frac{1}{2}(2ut + at^2)$ $\qquad$ $\boxed{s = ut + \frac{1}{2}at^2}$

This can also be found if we remember that the area under a velocity-time graph represents the distance travelled/displacement. The area under the line equals the area of rectangle A + the area of triangle B.

Area = Displacement = $s = ut + \frac{1}{2}(v-u)t$ since $a = \frac{(v-u)}{t}$ then $at = (v-u)$ so the equation becomes

$s = ut + \frac{1}{2}(at)t$ which then becomes equation 3

Equation 4

If we rearrange equation 1 into $t = \frac{(v-u)}{a}$ which we will then substitute into equation 2:

$s = \frac{1}{2}(u+v)t \rightarrow s = \frac{1}{2}(u+v)\frac{(v-u)}{a} \rightarrow as = \frac{1}{2}(u+v)(v-u) \rightarrow$

$2as = (v^2 + uv - uv - u^2) \rightarrow 2as = v^2 - u^2$ $\boxed{v^2 = u^2 + 2as}$

Any question can be solved as long as three of the variables are given in the question.
Write down all the variables you have and the one you are asked to find, then see which equation you can use.
These equations can only be used for motion with UNIFORM ACCELERATION.