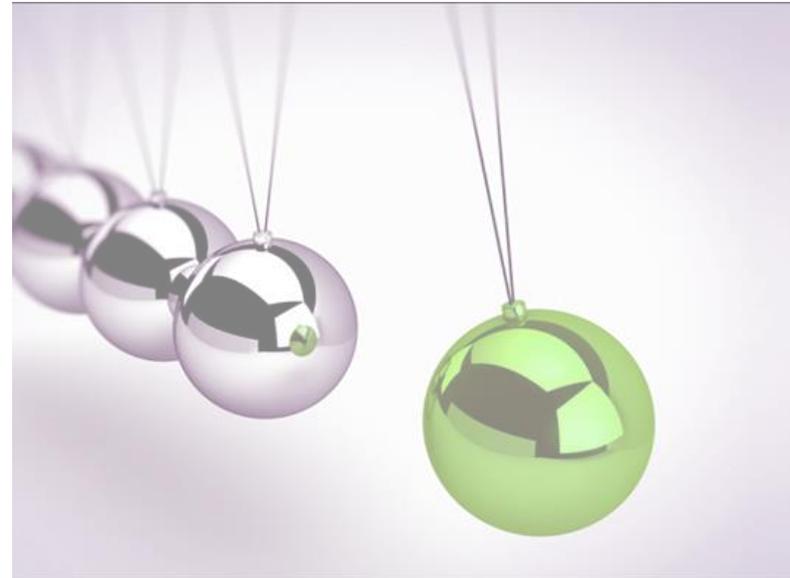


Mechanics & Materials

2015 AQA A Level Physics

**Momentum
and
collisions**



Momentum

An object having mass and velocity has **MOMENTUM**. Momentum (symbol “p”) is simply given by the formula:

$$\text{Momentum} = \text{Mass} \times \text{Velocity}$$

(in kgms⁻¹) (in kg) (in ms⁻¹)

What is the momentum of the following?

- 1) A 1kg football travelling at 10ms⁻¹
- 2) A 1000kg Ford Capri travelling at 30ms⁻¹
- 3) A 20g pen being thrown across the room at 5ms⁻¹
- 4) A 70kg bungi-jumper falling at 40ms⁻¹

Conservation of Momentum

The Principle of the Conservation of Momentum: In any collision or explosion momentum is conserved, provided that no external forces have an effect.

Two cars are racing on the motorway. Car A collides with the back of car B and the cars stick together. What speed do they move at after the collision?



Mass = 1000kg

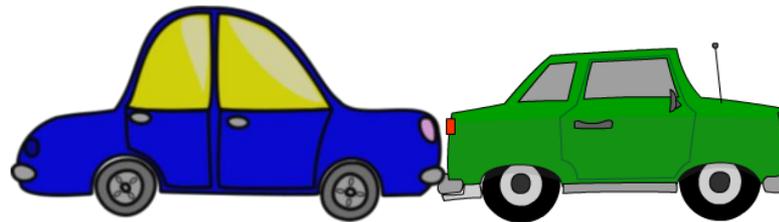
Speed = 60ms^{-1}



Mass = 700kg

Speed = 20ms^{-1}

Mass = 1700kg



Speed = $??\text{ms}^{-1}$

Momentum before = momentum after...

...so $(1000 \times 60) + (700 \times 20) = 1700 \times V$...

$V = 43.5 \text{ms}^{-1}$

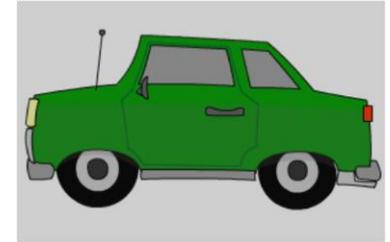
Momentum in different directions

What happens if the bodies are moving in opposite directions?



Speed = 60ms^{-1}

Speed = 20ms^{-1}



Momentum is a **VECTOR** quantity, so the momentum of the second car is negative...

Total momentum = $(1000 \times 60) - (700 \times 20) = 46000 \text{ kgms}^{-1}$

Speed after collision = $46000 \text{ kgms}^{-1} / 1700 = \mathbf{27.1\text{ms}^{-1}}$

More questions...

- 1) A white snooker ball moving at 6ms^{-1} strikes a red ball and pots it. Both balls have a mass of 1.5kg . If the white ball continued in the same direction at 2ms^{-1} what was the velocity of the red ball?
- 2) A car of mass 900kg heading up the M1 at 70ms^{-1} collides with a stationary truck of mass 8500kg and sticks to it. What velocity does the wreckage move forward at?
- 3) A defender running away from a goalkeeper at 5ms^{-1} is hit in the back of his head by the goal kick. The ball stops dead and the player's speed increases to 6.6ms^{-1} . If the ball had a mass of 700g and the player had a mass of 60kg how fast was the ball moving?
- 4) A gun has a recoil speed of 3ms^{-1} when firing. If the gun has a mass of 2kg and the bullet has a mass of 12g what speed does the bullet come out at?

Newton's 2nd Law and Impulse

Instead of $F=ma$ Newton actually said that the force acting on an object is that object's rate of change of momentum. In other words...

$$\text{Force (in N)} = \frac{\text{Change in momentum (in kgms}^{-1}\text{)}}{\text{Time (in s)}}$$

Also called "impulse"

For example, Dimitri Payet takes a free kick by kicking a stationary football with a force of 50N. If the ball has a mass of 0.5kg and his foot is in contact with the ball for 0.1s calculate:

- 1) The change in momentum of the ball (its impulse),
- 2) The speed the ball moves away with

Example questions

- 1) Alice likes playing golf. She strikes a golf ball with a force of 85N. If the ball has a mass of 300g and the club is in contact with it for 0.3s calculate a) the change in momentum of the golf ball, b) its speed.
- 2) Sam thinks it's funny to hit tennis balls at Sean. He strikes a serve with a force of 35N. If the ball has a mass of 250g and the racket is in contact with it for 0.2s calculate the ball's change in momentum and its speed.
- 3) Dom takes a dropkick by kicking a 0.5kg rugby ball away at 13m/s. If his foot was in contact with the ball for 0.1 seconds calculate the force he applied to the ball.
- 4) Steve strikes a 200g golf ball away at 70ms^{-1} . If he applied a force of 60N calculate how long his club was in contact with the ball for.

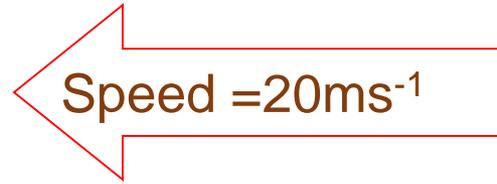
Another way to ask the same question...

Here's a situation we looked at earlier...



Mass = 1000kg

Speed = 60ms^{-1}



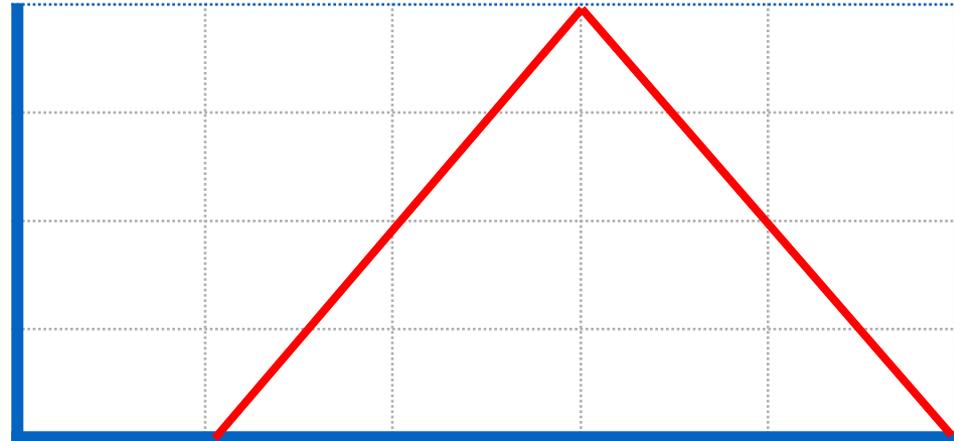
Mass = 700kg

Speed = 20ms^{-1}

What's the impulse of the car on the left if the cars stick together?

Calculate appropriate scales for the force-time graph shown.

Force

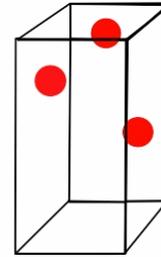


Time

Elastic and Inelastic collisions

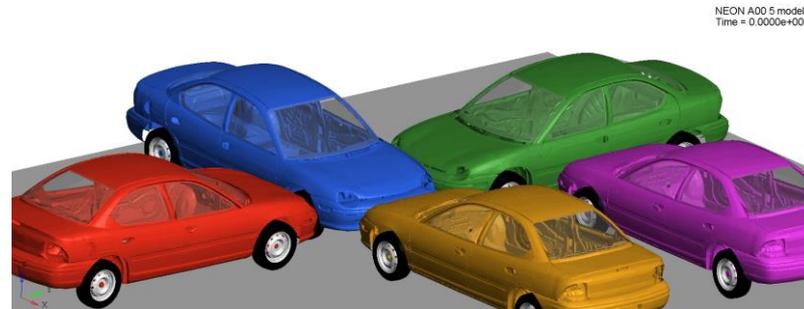
In an **elastic collision**, no kinetic energy is lost

Collisions between molecules in a gas can be treated as elastic



In an **inelastic collision**, kinetic energy is transferred to other energy stores

Collisions between everyday objects tend to generate sound and thermal energy and are therefore **inelastic**.



Elastic or inelastic?

Earlier we used conservation of momentum to calculate the velocity of the combined vehicles. Calculate the Kinetic energy before and after the collision

To determine whether the collision is elastic or inelastic



Mass = 1000kg

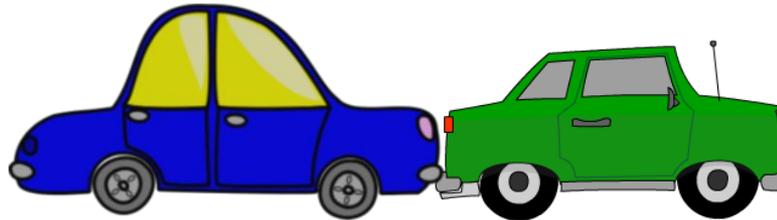
Speed = 60ms⁻¹



Mass = 700kg

Speed = 20ms⁻¹

Mass = 1700kg



Speed = 27.1ms⁻¹

Kinetic Energy before = $(\frac{1}{2} \times 1000 \times 60^2) + (\frac{1}{2} \times 700 \times 20^2) = 1.96\text{MJ}$

Kinetic Energy after = $\frac{1}{2} \times 1700 \times 27.1^2 = 1.61\text{MJ}$

Collision is **inelastic**; 0.35MJ shifted to other stores (thermal, sound)